Name:

| Problem | Points | Score |
| :--- | :--- | :--- |
| 1a | 10 |  |
| 1b | 10 |  |
| 1c | 10 |  |
| 1d | 10 |  |
| 2a | 10 |  |
| 2b | 10 |  |
| 2c | 10 |  |
| 3a | 10 |  |
| 3b | 10 |  |
| 3c | 10 |  |
| Total | 100 |  |

## Notes:

1. The exam is closed books/closed notes - except for one page of notes.
2. Please show ALL work. Incorrect answers with no supporting explanations or work will be given no partial credit.
3. Please indicate clearly your answer to the problem.

## Problem No. 1:


(a) Sketch the magnitude spectrum of $z(t)=x(t) w(t)$ for $a=1.5$ :
(b) Compare the result in part (a) to the result that woud be obtained if $w(t)$ is changed from a rectangular function to a triangle-shaped function:

(c) Name your favorite Fourier transform theorem:
(d) Prove the theorem described in (c):

## Problem No. 2:

(a) $x(t)$ is a data communications signal that has frequency content ranging from -75 Hz to 75 Hz . Compute $y(t)$ for the system shown below:

(b) Describe the shape of the magnitude spectrum of the impulse train shown below:

(c) Prove that the principles of linearity and superposition hold for the Fourier Transform:

Problem No. 3:

(a) Compute $\mathrm{H}_{1}(\mathrm{~s}), \mathrm{H}_{2}(\mathrm{~s})$, and $\mathrm{H}_{1}(\mathrm{~s}) \mathrm{H}_{2}(\mathrm{~s})$. Assume all initial conditions are zero.
(b) Compute the transfer function $\mathrm{H}(\mathrm{s})$. Assume all initial conditions are zero.

(c) Explain the similarities and differences between $H_{1}(s) H_{2}(s)$ in (a) and the answer to (b). Are these systems linear?

