

Common Fourier Transform Pairs

$f(t), \quad a > 0, \tau > 0$	$F(\omega)$
$e^{-at}u(t)$	$\frac{1}{a + j\omega}$
$te^{-at}u(t)$	$\left(\frac{1}{a + j\omega}\right)^2$
$p_\tau(t) = \begin{cases} 1, & -\frac{\tau}{2} \leq t < \frac{\tau}{2}, \\ 0, & \text{else} \end{cases}$	$\tau \operatorname{sinc}\left(\frac{\tau\omega}{2\pi}\right)$
$\Delta_\tau(t) = \begin{cases} 1 - \frac{2 t }{\tau}, & -\frac{\tau}{2} \leq t < \frac{\tau}{2} \\ 0, & \text{else} \end{cases}$	$\frac{\tau}{2} \operatorname{sinc}^2\left(\frac{\tau\omega}{4\pi}\right)$
$e^{-a t }$	$\frac{2a}{a^2 + \omega^2}$
$e^{-at} \sin(\omega_0 t) u(t)$	$\frac{\omega_0}{(a + j\omega)^2 + \omega_0^2}$
$e^{-at} \cos(\omega_0 t) u(t)$	$\frac{a + j\omega}{(a + j\omega)^2 + \omega_0^2}$
e^{-at^2}	$\sqrt{\frac{\pi}{a}} e^{-\omega^2/4a}$
$\operatorname{sinc}\left(\frac{\tau t}{2\pi}\right)$	$\frac{2\pi}{\tau} p_\tau(\omega)$
$\operatorname{sinc}^2\left(\frac{\tau t}{4\pi}\right)$	$\frac{4\pi}{\tau} \Delta_\tau(\omega)$
$\frac{1}{a^2 + t^2}$	$\frac{\pi}{a} e^{-a \omega }$
$\delta(t)$	1
1	$2\pi\delta(\omega)$
$u(t)$	$\pi\delta(\omega) + \frac{1}{j\omega}$
$e^{j\omega_0 t}$	$2\pi\delta(\omega - \omega_0)$
$\cos(\omega_0 t)$	$\pi [\delta(\omega + \omega_0) + \delta(\omega - \omega_0)]$
$\sin(\omega_0 t)$	$j\pi [\delta(\omega + \omega_0) - \delta(\omega - \omega_0)]$
$\operatorname{sgn}(t) = \begin{cases} \frac{t}{ t }, & t \neq 0, \\ 0, & t = 0 \end{cases}$	$\frac{2}{j\omega}$
$\cos(\omega_0 t)u(t)$	$\frac{\pi}{2} [\delta(\omega - \omega_0) + \delta(\omega + \omega_0)] + \frac{j\omega}{\omega_0^2 - \omega^2}$
$\sin(\omega_0 t)u(t)$	$\frac{\pi}{j2} [\delta(\omega - \omega_0) - \delta(\omega + \omega_0)] + \frac{\omega_0}{\omega_0^2 - \omega^2}$