

Fourier Transform Properties

$$\begin{aligned}
x(t) &\longleftrightarrow X(\omega) \\
X(t) &\longleftrightarrow 2\pi x(-\omega) \\
ax(t) + by(t) &\longleftrightarrow aX(\omega) + bY(\omega) \\
x(t - \tau) &\longleftrightarrow e^{-j\omega\tau}X(\omega) \\
x(at) &\longleftrightarrow \frac{1}{|a|}X\left(\frac{\omega}{a}\right) \\
x(-t) &\longleftrightarrow X(-\omega) \\
e^{j\omega_0 t}x(t) &\longleftrightarrow X(\omega - \omega_0) \\
x(t)\cos(\omega_0 t) &\longleftrightarrow \frac{1}{2}[X(\omega + \omega_0) + X(\omega - \omega_0)] \\
x(t)\sin(\omega_0 t) &\longleftrightarrow \frac{j}{2}[X(\omega + \omega_0) - X(\omega - \omega_0)] \\
t^n x(t) &\longleftrightarrow j^n \frac{d^n}{d\omega^n}X(\omega) \\
\frac{d^n}{dt^n}x(t) &\longleftrightarrow (j\omega)^n X(\omega) \\
\int_{-\infty}^t x(\lambda) d\lambda &\longleftrightarrow \frac{1}{j\omega}X(\omega) + \pi X(0)\delta(\omega) \\
x(t) * y(t) &\longleftrightarrow X(\omega)Y(\omega) \\
x(t)y(t) &\longleftrightarrow \frac{1}{2\pi}[X(\omega) * Y(\omega)] \\
\int_{-\infty}^{\infty} x(t)y(t) dt &\longleftrightarrow \frac{1}{2\pi} \int_{-\infty}^{\infty} \overline{X(\omega)}Y(\omega) d\omega \quad (\text{generalized Parseval's Theorem}) \\
\int_{-\infty}^{\infty} x^2(t) dt &\longleftrightarrow \frac{1}{2\pi} \int_{-\infty}^{\infty} |X(\omega)|^2 d\omega \quad (\text{Parseval's Theorem})
\end{aligned}$$