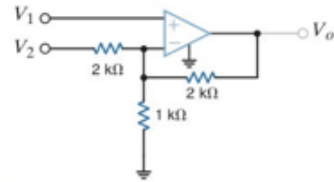


### Problem #1

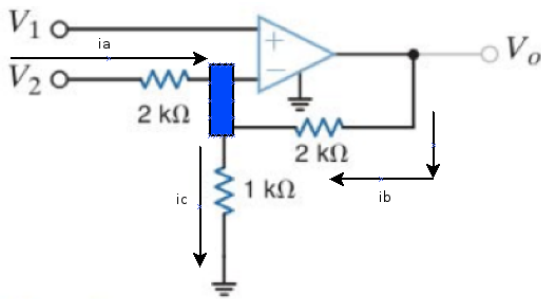
1. Derive an expression for  $V_o$  as a function of  $V_1$  and  $V_2$ .



#### Step 1.

Know that  $V_+ = V_- = v_1$

#### Step 2. Label each current



#### Step 3. Define the currents

$$i_a = (v_2 - v_1) / 2$$

$$i_b = (v_o - v_1) / 2$$

$$i_c = (v_1 - v_g) = v_1$$

#### Step 4. Do KCL for the blue node

$$i_a + i_b = i_c$$

$$(v_2 - v_1) / 2 + (v_o - v_1) / 2 = v_1$$

#### Step 5.

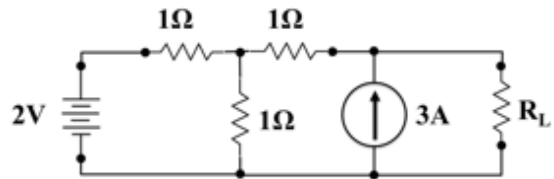
Solve for  $v_o$

Solve for  $v_o$  in terms of  $v_1$  and  $v_2$

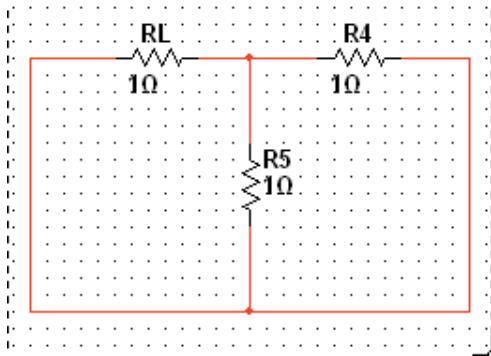
**Answer:**  $v_o = 4v_1 - v_2$

## Problem #2

2. (a) Using superposition, find the value of  $R_L$  that maximizes the power dissipated in  $R_L$ . Compute the portion of this power due to the voltage source only, and the portion due to the current source.



Step 1) Find  $R_{th}$  by shorting the voltage source and removing the current source.



This becomes  $R_{th} = 3/2$ .

Step 2) Remove the current source and solve for the load across the Resistor Load.  $V_L$ .

Use KCL to solve for  $V_1$  by finding all of the currents.

- $i_1$  (current from 2v source through  $R_4$ )
- $i_2$  (current between top node through  $R_6$  to ground)
- $i_3$  (current between top node through  $R_5$  to ground)

$$i_1 = (2 - V_a)$$

$$i_2 = V_a - \text{Ground} = V_a$$

$$i_3 = V_a$$

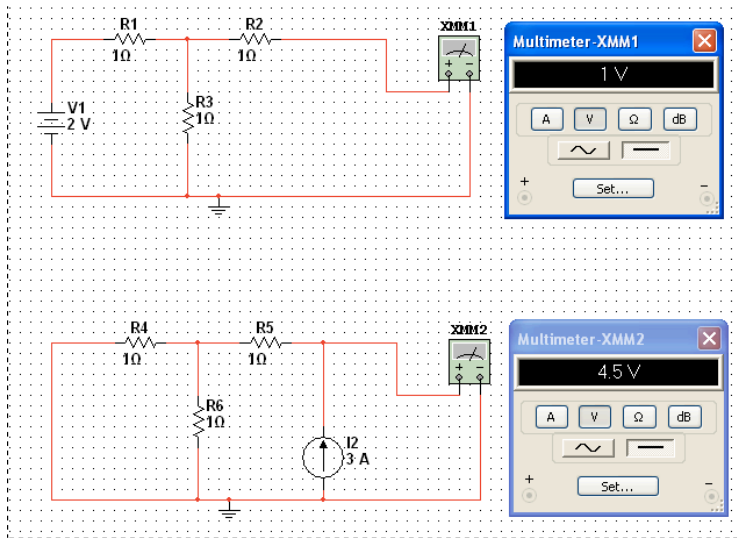
KCL at  $V_a$ :

We now know that  $V_a = 2/3$  and we can now use the the voltage divider to determine what it would be through the 1 Ohm resistor leading to our  $R_L$ .

$$V_L = 1 \text{ V}$$

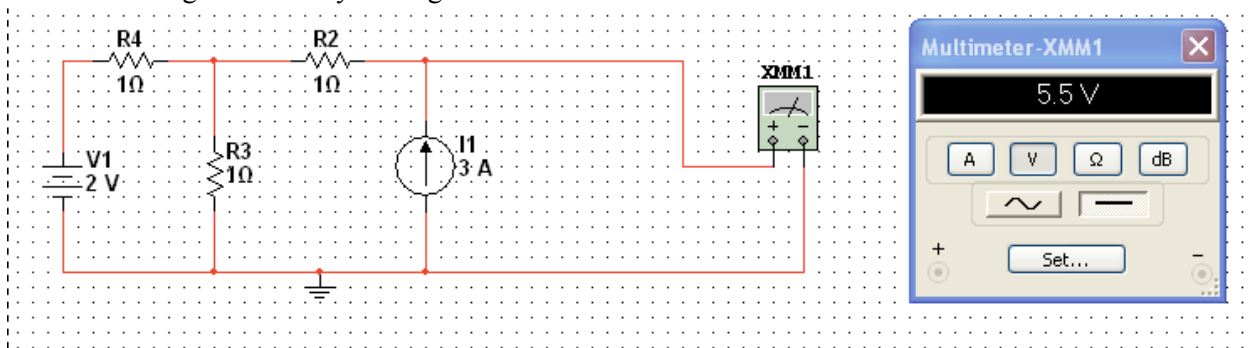
Step 3) Short the voltage source and solve for the load across the Resistor Load.  $V_L$ . Combine the resistors and determine the voltage through  $V_L$  to be 4.5.

$$V_L = 4.5$$

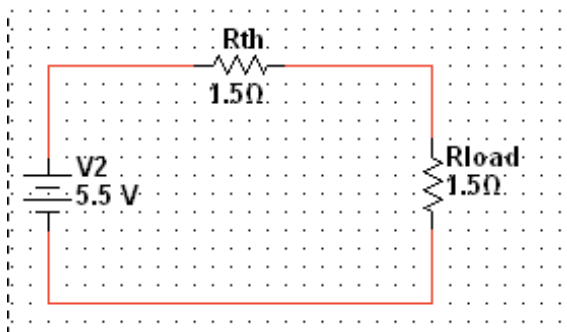


Step 4) Add both of the voltages found together to find  $V_L = 5.5$

The below image verifies my findings.



Step 5) Redraw the Thevenin equivalent circuit using  $V_L = 5.5$  and  $R_{th} = 3/2$



ANSWER:

See that we make the  $R_{load} = R_{th}$  because this is when maximum power happens, so  **$R_{load} = 1.5$** .

**Problem 2b**

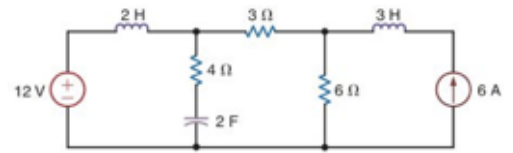
**2(b).** Remove the current source by treating it as an open circuit. Find the value of  $R_L$  that maximizes the power dissipated in  $R_L$ . Explain why this value is the same, or different, than the answer to (a). Justify your conclusion whether it should be the same or different.

ANSWER:

Our answers would be the same because our process would be quite similar. Instead of using the thevenin equivalent we would be finding the norton equivalent instead. All of our answers are identical because in circuits it does not matter which way we analyze anything as long as it works, many tools can be used for the same job. It is up to us to choose the one that we are best at or is most simple to use.

### PROBLEM #3

3. Find the energy stored in the 2F capacitor and 3H inductor.  
(Hint: find all voltages and currents first.)

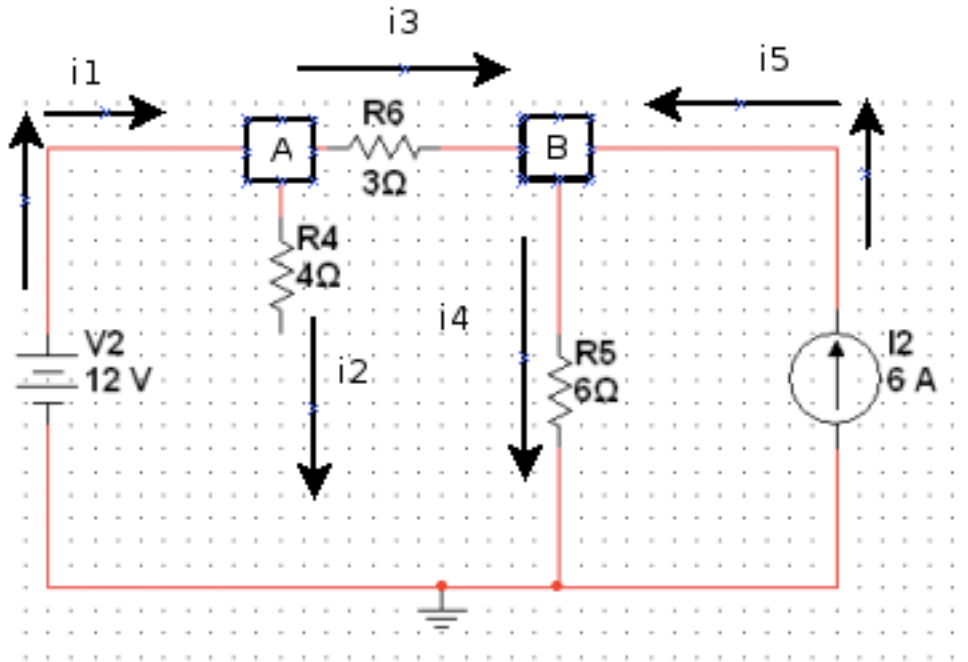


#### Step 1.)

Short the inductors and open the capacitors.

#### Step 2.)

Define the currents and label nodes.



$$i_1 = i_3$$

$$i_2 = 0$$

$$i_3 = (12 - v_b)/3$$

$$i_4 = (v_b - v_g)/6$$

$$i_5 = 6$$

#### Step 3.)

KCL for node A and node B

Node A:

$$i_1 = i_2 + i_3$$

$$i_1 = i_3$$

Replace  $i_3$  w/  $(12 - v_b)/3$

$$i_1 = (12 - v_b)/3$$

Node B:

$$i_3 + i_5 = i_4$$

$$(12 - v_b)/3 + 6 = v_b / 6$$

#### Step 4.)

Solve for unknowns:

$$v_b = 20\text{v}$$

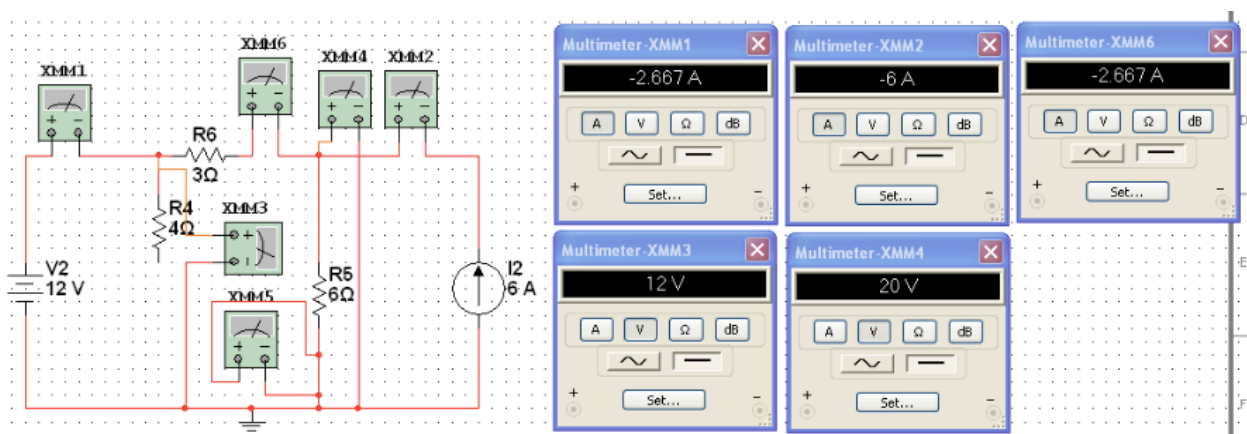
$$v_a = 12\text{v}$$

$$i_1 = i_3 = -8/3$$

$$i_3 = -8/3$$

$$i_4 = 10/3$$

$$i_5 = 6$$



**Step 5.)**

Use the information found in step 4 to solve for the energy stored in each component.

Find the energy stored in the capacitor via the following equation.

$$U = (1/2)(C)(V^2)$$

Answer:

$$U = (1/2)(2)(12^2) = 144.$$

Find the energy stored in the 3H inductor via the following equation.

$$U = (1/2)(L)(I^2)$$

Answer:

$$U = (1/2)(3)(6^2) = (3/2)(36) = 54.$$

Find the energy stored in the 2H inductor via the following equation.

$$U = (1/2)(L)(I^2)$$

Answer:

$$U = (1/2)(2)(-8/3)^2 = 7.111111 \text{ repeated}$$