LPC CODING OF SPEECH USING A NOVEL EXCITATION MODEL

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ABSTRACT

The quality of low bit rate speech using linear prediction is largely dependent on the model used for the excitation signal. In this paper a new Linear Predictive Coding (LPC) excitation model is introduced. This excitation model is composed of a set of orthogonal functions called zinc functions that are well-suited for modeling the LPC residual signal. The zinc basis functions are used in a low bit rate, multi-pulse LPC speech coding system. Results show that, given a fixed segmental signal-to-noise ratio, with similar computational complexity, the Zinc Multi-Pulse LPC (ZMPLPC) system is more efficient than a conventional Multi-Pulse LPC (MPLPC) system. Subjective listening tests also indicate a preference for the ZMPLPC system.

I. Introduction

Linear Predictive Coding (LPC) provides one of the most powerful methods for efficient coding of speech. At bit rates of 2.4-9.6 kbits/s, well below bit rates associated with conventional speech coding techniques (e.g., 64 kbits/s for PCM and 32 kbits/s for ADPCM), LPC speech is often characterized as being highly intelligible although below toll quality.

Linear predictive coding of speech is a source encoding method whereby the human speech production mechanism is modeled as a spectrally white glottal excitation signal applied to a vocal tract that acts like a filter superimposing a formant structure (or resonances) on the excitation to generate speech [1]. The glottal excitation signal is generated by the regular opening and closure of the vocal cords during voiced speech and by the relaxation of the vocal cords during unvoiced speech. The vocal tract is modeled by an all-pole filter that is excited by an excitation signal called the LPC excitation.

The quality of LPC speech is directly related to the model used for the LPC excitation signal. It has been shown [2-5] that improving the model used for the LPC excitation has a definite impact on the quality of the LPC synthetic speech. Some of the widely used models are given in [2-10] and include, the ideal impulse train model, the glottal pulse model [3], the mixed excitation model [4], the Fourier series model [6], the chirp signal model [8], the multi-pulse model [9], and the code excitation model [10].

In this paper a new LPC excitation model is presented, based on representing the LPC excitation with a set of basis functions, called zinc functions. The zinc functions are studied and a benchmark comparison between zinc function and Fourier series modeling of the LPC excitation is given. A multi-pulse system where the LPC excitation is constructed using the zinc basis functions instead of the conventional ideal impulses is presented; and improvements in speech quality and segmental signal-to-noise ratio over a conventional multi-pulse system are shown.

II. Zinc Function Decomposition of a Band-Limited Signal

Signal representation (or modeling) based on orthogonal function decomposition provides a very attractive method for quantitatively representing a given signal. Using a finite set of orthogonal zinc functions with similar characteristics to the excitation signal, we are able to greatly reduce the modeling error. Two important characteristics of the voiced LPC excitation are that they are band-limited and pulse-like. It is therefore desirable to represent these signals with a set of basis functions that are also band-limited and pulse-like.

The zinc function is defined as

$$z(t) = A\ \mathrm{Sinc}(t) + B\ \mathrm{Cosc}(t), \tag{1}$$

where

$$\mathrm{Sinc}(t) = [\sin(2\pi f_c t)]/2\pi f_c t, \tag{2}$$

and

$$\mathrm{Cosc}(t) = [1-\cos(2\pi f_c t)]/2\pi f_c t. \tag{3}$$

Here A, B, and f_c ($= 1/T_c$) are constants. Time domain characteristics of the zinc function are shown in Fig. 1, and it is easy to show that the spectrum of z(t) is given by

$$\begin{aligned} |Z(f)| &= (A^2 + B^2)^{1/2}, && |f| < f_c, \\ &= 0, && |f| > f_c, \end{aligned} \tag{4}$$

and

$$\arg Z(f) = -\ \mathrm{sgn}(f)\ \tan^{-1}(B/A). \tag{5}$$

Clearly z(t) is pulse-like and band-limited, with the cutoff frequency being f_c.

Our goal is to obtain a family of zinc functions that are orthogonal and complete. For this purpose let us define a set of functions consisting of time-shifted zinc functions, that is,

$$z_n(t) = A_n\ \mathrm{Sinc}(t - \lambda_n) + B_n\ \mathrm{Cosc}(t - \lambda_n). \tag{6}$$

The orthogonality property of the functions in Eq. (6) is dependent on the parameter λ_n. It can be shown [11] that if λ_n is set to nT_c, where n is any integer, then the resulting set of zinc functions in Eq. (6) are orthogonal. Note also that each zinc function is itself composed of two orthogonal functions, namely Sinc(t) and Cosc(t).

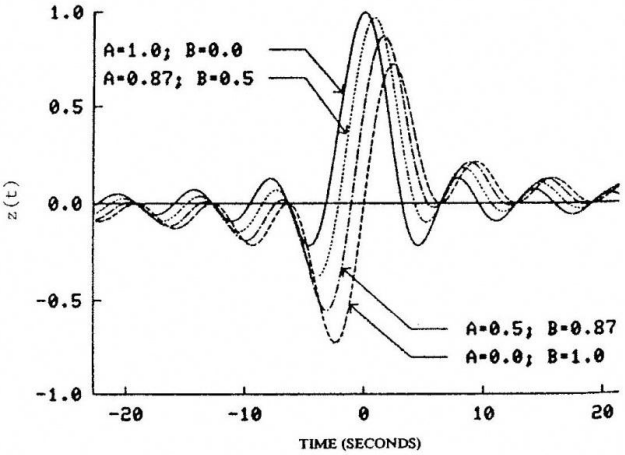

Figure 1. Zinc Function Time Domain Characteristics (where $A^2 + B^2 = 1$ and $2\pi f_c = 1$).

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Now we shall show, by contradiction, that the orthogonal set of zinc functions is complete spanning the space of all band-limited signals. Assume the zinc basis functions do not form a complete set over the intended space. This implies that there exists a band-limited signal, $x(t)$, that cannot be exactly represented by an infinite sum of weighted orthogonal zinc functions. This in turn implies that there exists a non-zero error signal, $\epsilon(t)$, such that

$$x(t) = r(t) + \epsilon(t), \tag{7}$$

where

$$r(t) = \sum_{n=-\infty}^{\infty} A_n \, \mathrm{Sinc}(t - nT_n) + B_n \, \mathrm{Cosc}(t - nT_n). \tag{8}$$

To define $r(t)$ uniquely, f_c, $\{A_n\}$, and $\{B_n\}$ need to be determined. Given the zinc function frequency characteristics, it is clear that f_c should be set to the cutoff frequency of $x(t)$. The remaining parameters, $\{A_n\}$ and $\{B_n\}$, are determined by minimizing the mean-squared of the error signal $\epsilon(t)$. Using the orthogonality properties, the minimization yields

$$A_n = 2f_c \int_{-\infty}^{\infty} x(t) \, \mathrm{Sinc}(t - nT_c) \, dt, \tag{9}$$

and

$$B_n = 2f_c \int_{-\infty}^{\infty} x(t) \, \mathrm{Cosc}(t - nT_c) \, dt. \tag{10}$$

The Fourier transform of $r(t)$ can now be written as

$$R(\omega) = \sum_{n=-\infty}^{\infty} C_n \, e^{-j\theta_n} e^{-j\omega nT_c}, \qquad 0 < \omega < 2\pi f_c, \tag{11}$$

$$= \sum_{n=-\infty}^{\infty} C_n \, e^{j\theta_n} e^{-j\omega nT_c}, \qquad -2\pi f_c < \omega < 0,$$

$$= 0, \qquad \text{elsewhere.}$$

where

$$C_n = 0.5T_c(A_n^2 + B_n^2)^{1/2}, \tag{12}$$

and

$$\theta_n = \tan^{-1}(B_n/A_n). \tag{13}$$

It can be shown [11] that the Fourier transform of any band-limited signal (with cutoff frequency of f_c) can be expressed *exactly* using Eqs. (11-13) where A_n and B_n are computed from Eqs. (9) and (10), respectively. The proof for this can be arrived at by expressing the Fourier transform of $x(t)$ using a Fourier series in the frequency band $(-f_c, f_c)$, and then comparing terms with Eq. (11).

This proof implies that $X(\omega) \equiv R(\omega)$ or $r(t) \equiv x(t)$. This in turn requires that $\epsilon(t) \equiv 0$, contradicting our assumption that $\epsilon(t)$ is non-zero. We therefore conclude that the zinc basis functions, given in Eq. (6), form a complete orthogonal set. Thus, any band-limited signal, $x(t)$, can now be represented as in Eq. (8).

III. Zinc Function versus Fourier Series Modeling

Having shown that the zinc functions form a complete orthogonal set, and that they are inherently well-suited for efficient modeling of the LPC excitation, we shall now compare the performance of zinc function modeling with the performance of Fourier series modeling.

A voiced residual frame and three zinc function model signals are shown in Fig. 2, where the model order is 5, 10, and 15. The zinc function parameters for the model signals were obtained by minimizing the mean-squared error for the particular model order. Observe the ability of the zinc functions to closely model the perceptually important pitch pulses with a relatively low-order model. The same voiced frame is shown in Fig. 3 with three Fourier series model signals, again with model order 5, 10, and 15 where the mean-squared error criteria was minimized. Note that both basis function models require the same number of parameters to describe the signal. It is clear from Figs. 2 and 3, that the zinc function model is superior to the Fourier series model given the same model order.

Quantitatively, a measure of the goodness of the model is the signal-to-noise ratio (SNR) between the residual and the model signal. The SNR of the zinc function and the Fourier series modeling methods were computer for a database consisting of 16 seconds of speech generated by 50 different speakers (25 male and 25 female). A comparison of the two modeling methods for voiced and unvoiced frames is shown in Fig. 4. The SNR values in these figures are averaged over all 20 msec. frames in the database. In the case of voiced frames, the zinc function representation is significantly better than the Fourier series representation for a given model order, but only marginally better in the unvoiced case. This result makes intuitive sense since both the voiced residual and the zinc functions are pulse-like signals while the unvoiced residual is similar to white noise.

IV. The Zinc Multi-Pulse LPC (ZMPLPC) System

The block diagram of the ZMPLPC system is depicted in Fig. 5. The ZMPLPC system is an extension of the conventional MPLPC system [9], where now zinc basis functions are used in constructing the LPC excitation. The ZMPLPC system has the ability to adjust the zinc pulse shape to optimally represent the pulses in the LPC excitation.

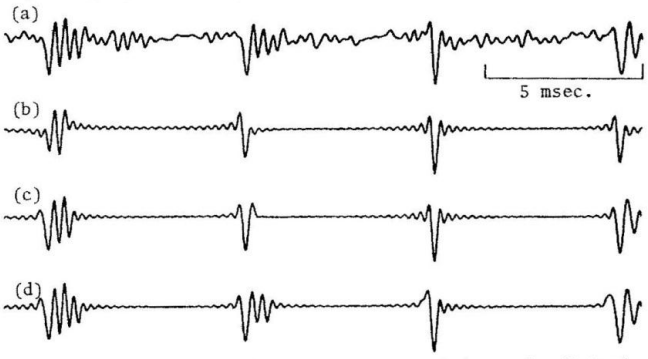

Figure 2. An Example of Zinc Function Modeling of a Voiced Frame: (a) Original Residual (20 msec. Duration); (b) 5th Order Model; (c) 10th Order Model; (d) 15th Order Model.

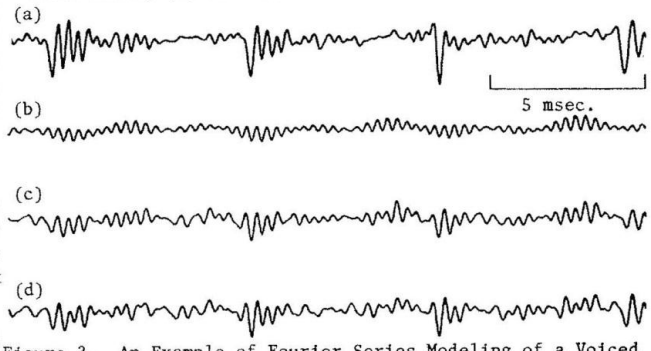

Figure 3. An Example of Fourier Series Modeling of a Voiced Frame: (a) Original Residual (20 msec. Duration); (b) 5th Order Model; (c) 10th Order Model; (d) 15th Order Model.

At each stage of the analysis-by-synthesis process, the noise weighted error is minimized to obtain the parameters of a new zinc function to be added to the excitation of the previous stage. The k^{th} stage error signal, $\hat{e}^{(k)}(n)$, can be expressed as,

$$\hat{e}^{(k)}(n) = s_0(n) - \sum_{i=1}^{k} z_i(n) * h(n), \tag{14}$$

where,

$$z_i(n) = A_i \, \mathrm{Sinc}(n - \lambda_i) + B_i \, \mathrm{Cosc}(n - \lambda_i). \tag{15}$$

Here $s_0(n)$ is the original speech signal with the previous frame's synthesis filter contribution removed, $\{\lambda_i\}$ are the zinc function locations, and $h(n)$ is the impulse response of the synthesis filter $H(z)$. The zinc function cutoff frequency is set at 4 kHz.

The $(k+1)^{st}$ zinc function parameters (A_{k+1}, B_{k+1}, and λ_{k+1}) are determined by minimizing the noise weighted mean-squared error. The noise weighted error can be expressed as,

$$\hat{e}_w^{(k+1)}(n) = \left[\hat{e}^{(k)}(n) * w(n)\right] - \left[z_{k+1}(n) * h(n) * w(n)\right], \tag{16}$$

where $w(n)$ is the impulse response of the perceptual noise weighting filter $W(z)$, as used in a conventional MPLPC system [9].

Minimizing the mean-squared noise weighted error, $\hat{e}_w^{(k+1)}(n)$, with respect to A_{k+1} and B_{k+1}, and simplifying yields

$$A_{k+1} = \frac{R_{es} R_{cc} - R_{ec} R_{cs}}{R_{ss} R_{cc} - (R_{cs})^2}, \tag{17}$$

and

$$B_{k+1} = \frac{R_{es} R_{ss} - R_{es} R_{cs}}{R_{ss} R_{cc} - (R_{cs})^2}, \tag{18}$$

where the terms in Eqs. (17) and (18) are modified zinc cross- and auto-correlation functions as detailed in [11]. A fair amount of elegant mathematics lucidly explained in [11] allows us to simplify Eqs. (17) and (18) to

$$A_{k+1} = R_{es}/R_{ss}, \tag{19}$$

and

$$B_{k+1} = R_{ec}/R_{cc}. \tag{20}$$

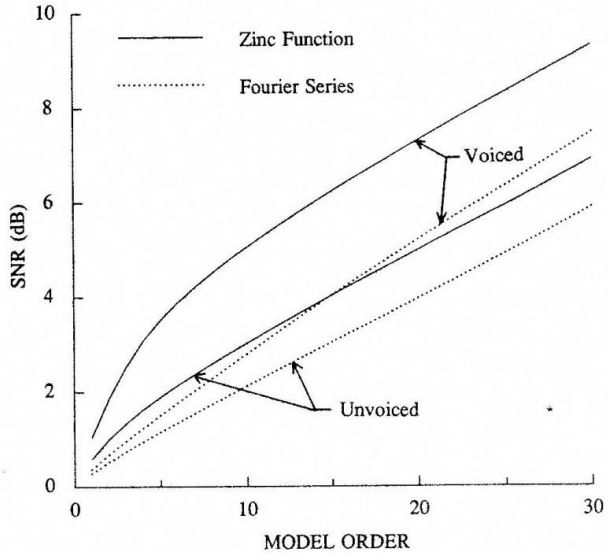

Figure 4. Comparison Between Zinc Function and Fourier Series Modeling of the LPC Residual (Voiced and Unvoiced Cases).

The term R_{es} is the average of $\hat{e}^{(k)}(n)$ after $w(n)$ filtering, with $\mathrm{Sinc}(n - \lambda_{k+1})$ after $h(n)$ and $w(n)$ filtering. The term R_{ec} has the same form as R_{es} except Cosc is used instead of Sinc. The term R_{ss} or R_{cc} is the average of the square of $\mathrm{Sinc}(n - \lambda_{k+1})$ or $\mathrm{Cosc}(n - \lambda_{k+1})$ after $h(n)$ and $w(n)$ filtering.

Similar to a conventional MPLPC system, the $(k+1)^{st}$ zinc location, λ_{k+1}, is determined by computing A_{k+1} and B_{k+1}, now only for every orthogonal location within the frame, and then setting λ_{k+1} to the location that results in a minimum mean-squared noise weighted error. Since the orthogonal locations are at nT_c and T_c is set to $T_s/2$, the exhaustive search need only be performed at alternate sample points, compared to every sample point for a conventional MPLPC system. This is a very important aspect of the ZMPLPC system since the amount of information needed to describe the *pulse locations* in the multi-pulse excitation is effectively reduced by a factor of two in comparison to a conventional MPLPC system. Another point to note about the ZMPLPC system is that its computational complexity is very close to the computational complexity of the well-known MPLPC system. The fact that only one half of the frame locations need to be searched, offsets the computations needed to find the two scalars A_{k+1} and B_{k+1}.

An example of the ZMPLPC excitation is shown in Fig. 6. The top signal is a typical voiced residual signal, while the bottom two signals are the MPLPC and ZMPLPC excitations respectively. Note that both types of excitations use the same number of pulses. Note also that the residual signal exhibits the sharp negative/positive swings usually found in the LPC voiced residual. The inherent flexibility of the zinc pulse in efficiently modeling these types of negative/positive swings makes the zinc basis functions attractive in a multi-pulse system.

A 58 speaker database, described in [12], representing a diverse population of speakers, was constructed to compare performance between conventional MPLPC and ZMPLPC. Each sample utterance in the database consisted of a short voiced segment excised from a Harvard phonetically balanced sentence.

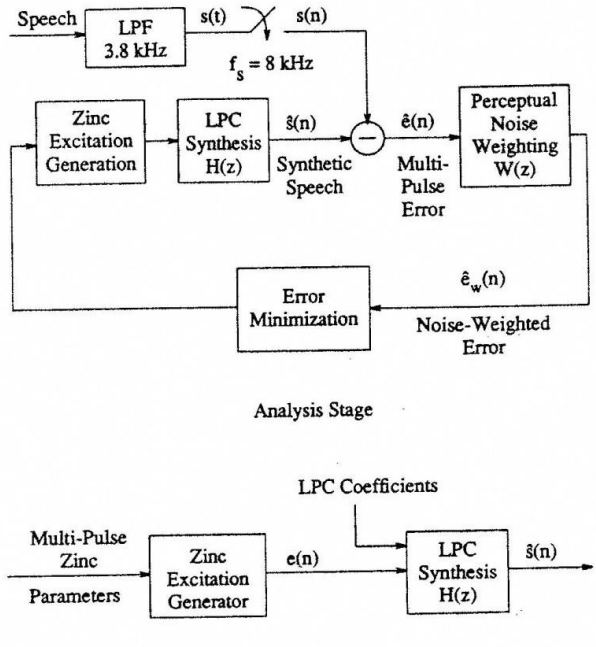

Figure 5. The Zinc Multi-Pulse LPC (ZMPLPC) System.

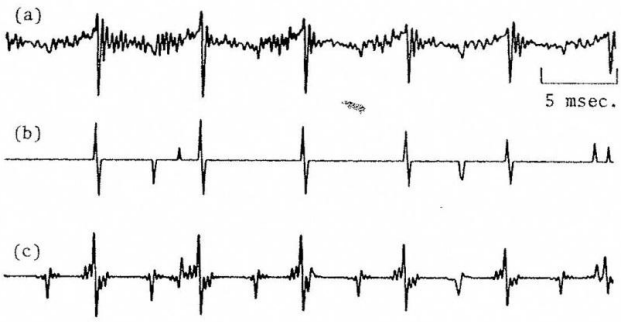

Figure 6. A Comparison Between the MPLPC and the ZMPLPC Excitations: (a) Original Residual (40 msec. Duration); (b) MPLPC Excitation; (c) ZMPLPC Excitation.

An objective comparison is seen from the segmental signal-to-noise ratio (SSNR), averaged over the entire database, of each system. The SSNR is plotted in Fig. 7 versus the number of pulses in a 5 msec. frame. Subjective listening tests also indicate a definite preference for the ZMPLPC system.

The comparative performance of these two systems ultimately must be measured at similar data rates. This requires us to consider the number of positions and amplitudes needed in MPLPC and ZMPLPC, as well as the position resolution needed. Although no complete coding scheme with bit allocations was implemented, bit rates are estimated in the range of 9.6 kbps (to a maximum of 16 kbps). Based on required amplitudes and positions, our experiments indicate that with simple coding techniques, approximately a 25% reduction in bit rate for the ZMPLPC system over conventional MPLPC can be achieved, and the same SSNR maintained. Further reductions in bit rate are possible by using the correlation in adjacent zinc pulse shapes.

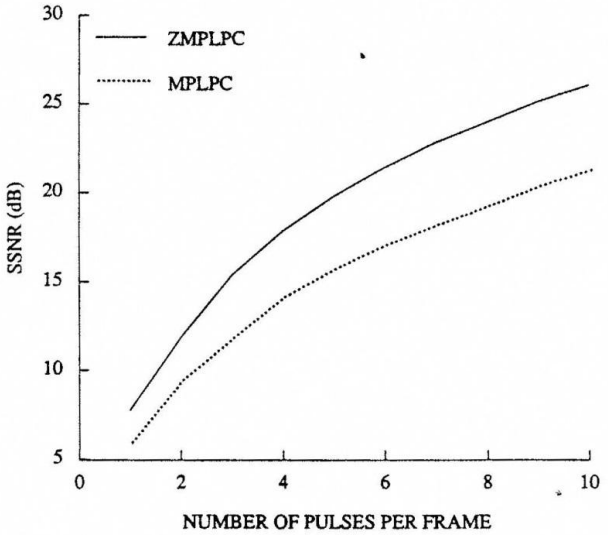

Figure 7. Segmental Signal-to-Noise Comparison Between ZMPLPC and MPLPC Systems.

V. Conclusions

This paper has presented a new model for the LPC excitation. The model excitation signal is composed of a complete set of orthogonal functions called zinc functions. The zinc basis functions were shown to have properties well-suited for efficient modeling of the LPC residual. The zinc function excitation model was used in a multi-pulse LPC system. The ZMPLPC system is shown to be more efficient with respect to the amount of information transmitted to the synthesizer in comparison to a conventional MPLPC system. This savings in transmitted information is achieved at a minimal increase in the number of computations.

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